

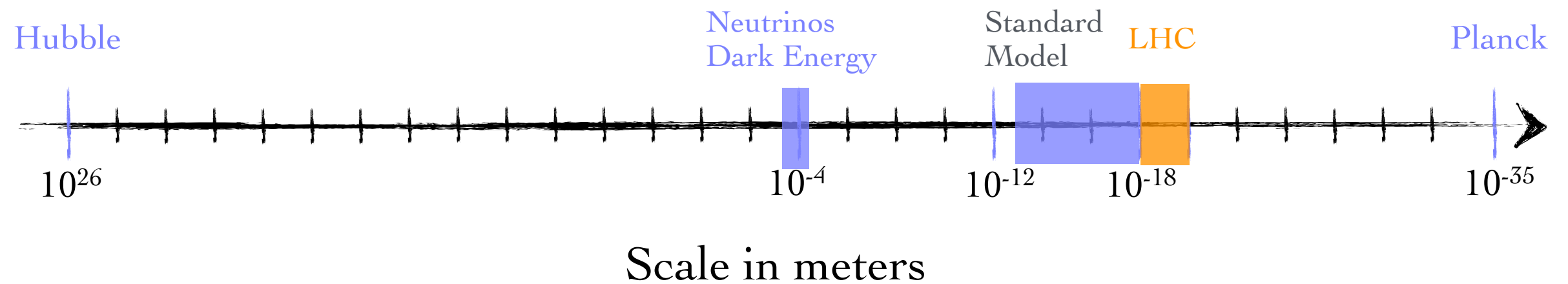
# The case for Ultra-Light Boson Dark Matter

Asimina Arvanitaki  
Perimeter Institute

# The High Energy Frontier



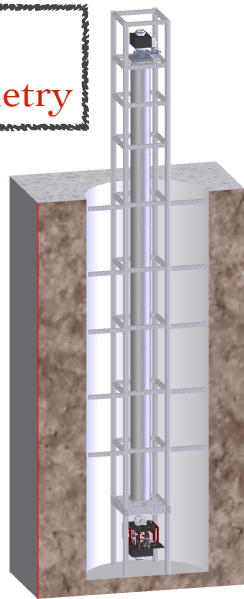
# Particle Physics — Precision vs Energy Frontier



*80% of scales unexplored*

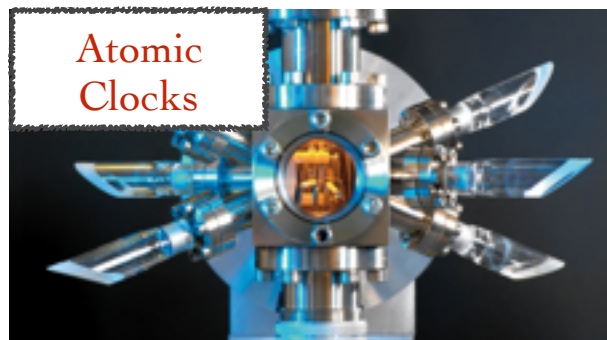
# Opportunities to probe the low energy frontier

## Atom Interferometry



- Tests of Gravity
- Gravitational Wave detection at low frequencies
- Tests of Atom Neutrality at 30 decimals

Dimopoulos, Geraci (2003)  
Dimopoulos, Kasevich et. al. (2006-2008)

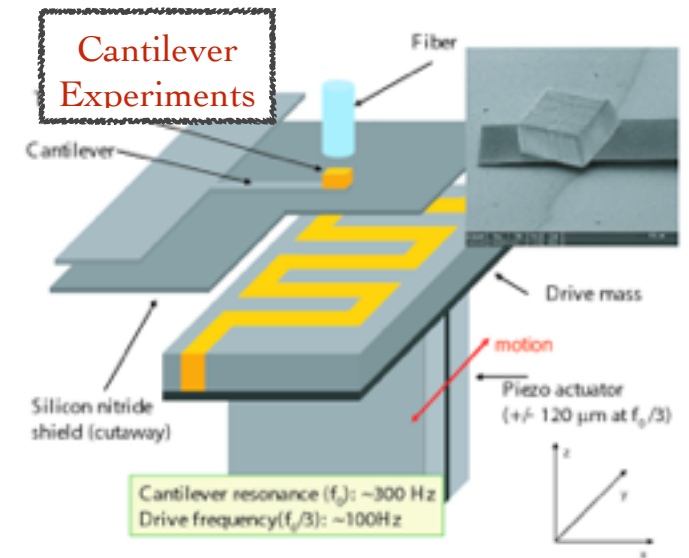


## Atomic Clocks

- Setting the Time Standard
- Dilaton Dark Matter Detection

AA, Huang, Van Tilburg (2014)

- Short Distance Tests of Gravity
- Extra Dimensions



Dimopoulos, Kapitulnik (1997)

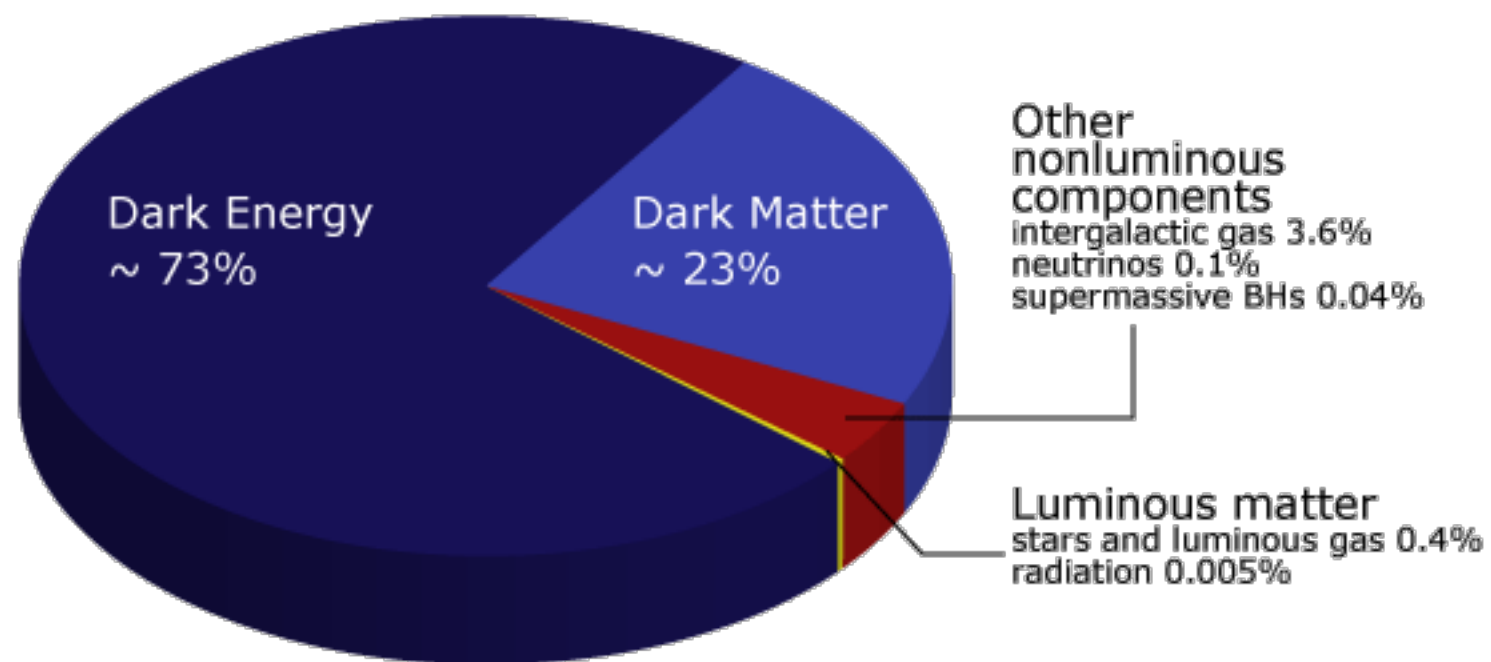
- Axion Dark Matter Detection
- Axion Force Detection



Graham et. al. (2012)  
AA, Geraci (2014)



# The Mystery of Dark Matter

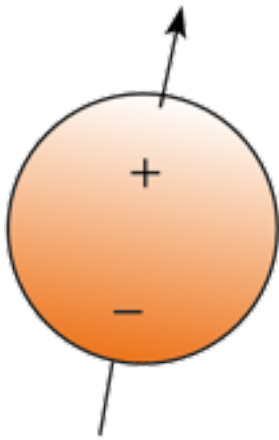


# Models of Dark Matter

- What is it made out of?
- How is it produced?
- Does it have interactions other than gravitational?

# Why is the Electric Dipole Moment of the Neutron Small?

The Strong CP Problem and the QCD axion



Neutron Electric Dipole Moment  
 $\sim e \text{ fm } \theta_{\text{QCD}}$

$$L_{\text{SM}} \supset \frac{g_s^2}{32\pi^2} \theta_{\text{QCD}} G^a \tilde{G}^a$$

Experimental bound:  $\theta_{\text{QCD}} < 10^{-10}$

Solution:

$\theta_{\text{QCD}}$  is a dynamical field, an axion

Weinberg(1978) and Wilczek (1978)  
Peccei and Quinn (1977)

Axion mass from QCD:

$$\mu_a \sim 6 \times 10^{-11} \text{ eV} \frac{10^{17} \text{ GeV}}{f_a} \sim (3 \text{ km})^{-1} \frac{10^{17} \text{ GeV}}{f_a}$$

$f_a$  : axion decay constant

# Elements of String Theory

- Extra dimensions



# Elements of String Theory

- Extra dimensions

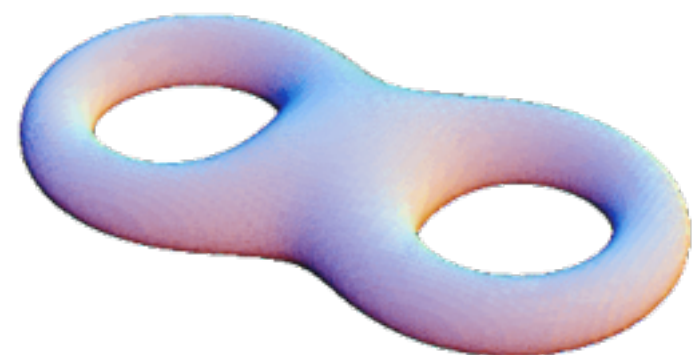
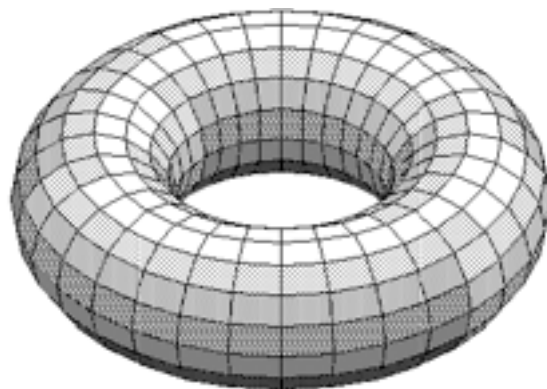
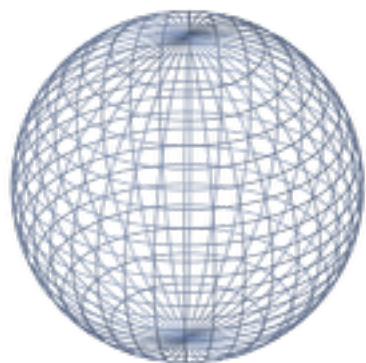
- Gauge fields

# Elements of String Theory

- Extra dimensions

- Gauge fields

- Topology

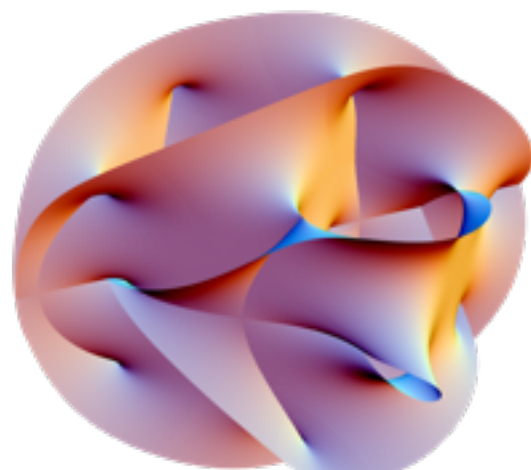


# Elements of String Theory

- Extra dimensions

- Gauge fields

- Topology



# Elements of String Theory

- Extra dimensions

- Gauge fields

- Topology



Give rise to a plenitude of Universes



# Elements of String Theory

- Extra dimensions

- Gauge fields

- Topology

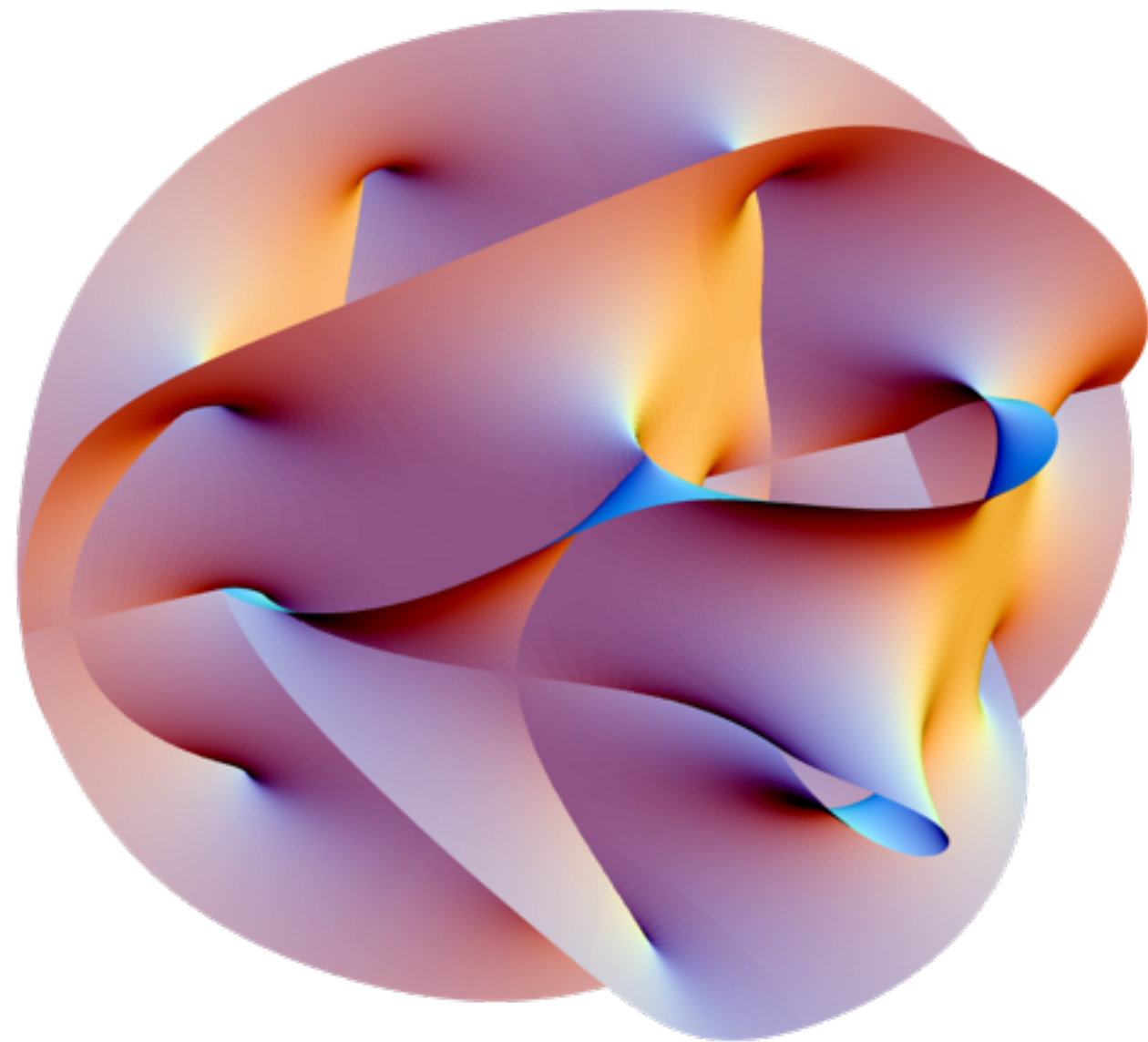


Give rise to a plenitude of massless particles in our Universe

# A Plenitude of Massless Particles

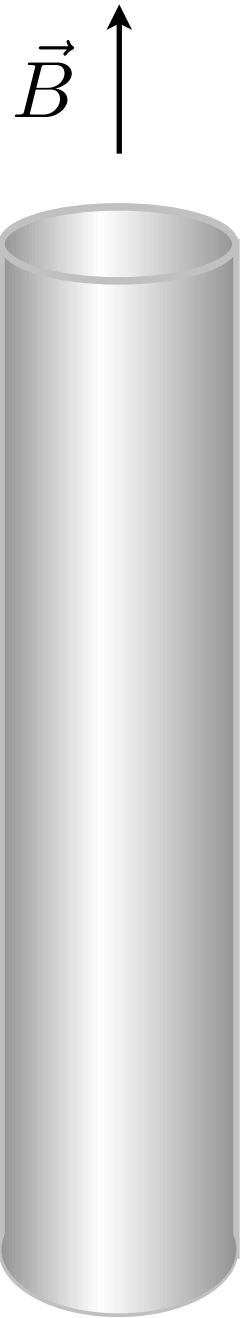
Compactification naturally gives rise to massless particles

In the presence of non-trivial topology,  
non-trivial gauge field configurations can carry no  
energy,  
resulting in 4D massless particles



# Non-trivial gauge configurations

## The Aharonov-Bohm Effect



Solenoid

Taking an electron around the solenoid

$$e \int A_\mu dx^\mu = e \times \text{Magnetic Flux}$$

while

$$\vec{B} = 0$$

Energy stored only inside the solenoid

Non-trivial gauge configuration far away carries no energy

# Non-trivial gauge configurations

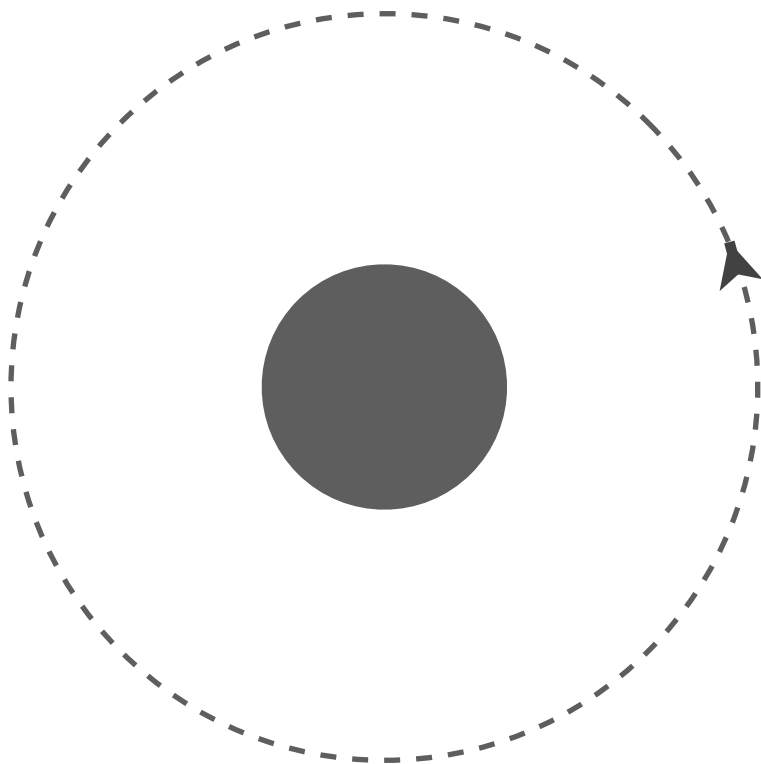
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# Non-trivial gauge configurations

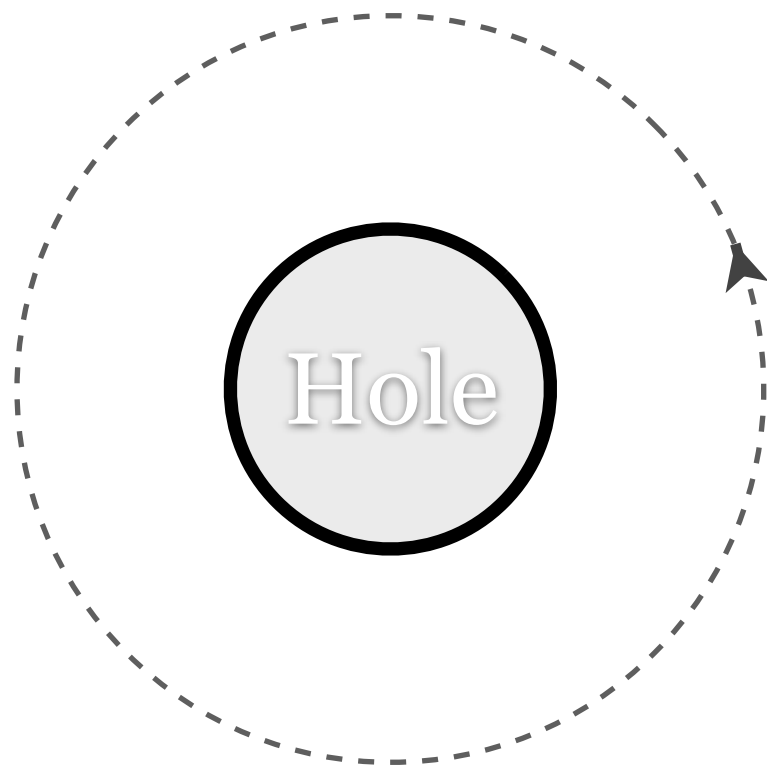
## The Aharonov-Bohm Effect

Taking an electron around the solenoid

$$e \int A_\mu dx^\mu = e \times \text{Magnetic Flux}$$

while

$$\vec{B} = 0$$



Non-trivial topology:

“Blocking out” the core still leaves a non-trivial gauge, but no mass

# A Plenitude of Massless Particles

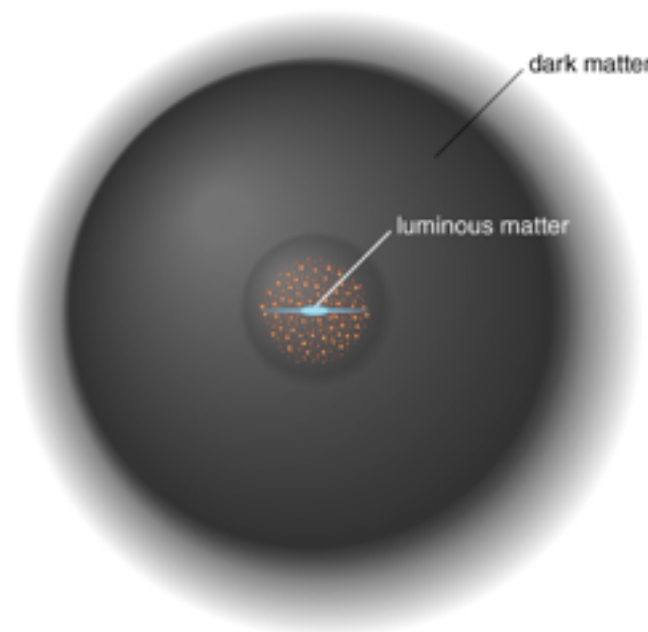
- Spin-0 non-trivial gauge field configurations: String Axiverse
- Spin-1 non-trivial gauge field configurations: String Photiverse
- Fields that determine the shape and size of extra dimensions as well as values of fundamental constants: Dilatons, Moduli, Radion

# Properties of Plenitude of Particles from String Theory

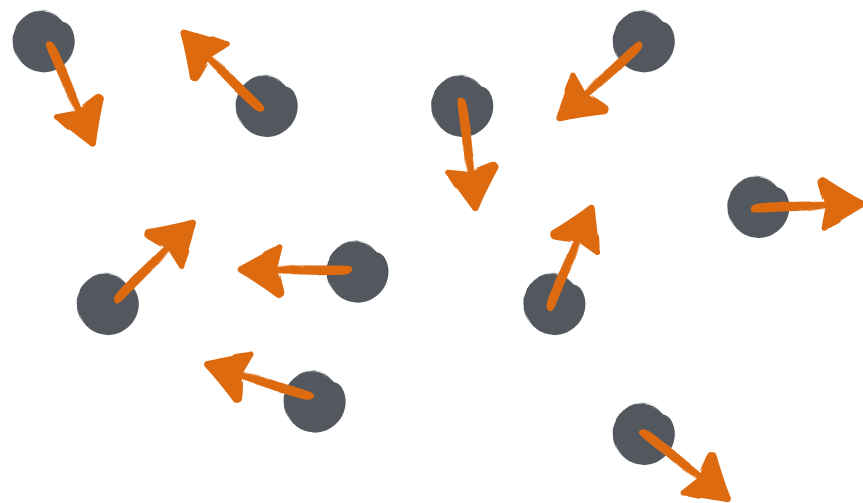
- They couple very weakly to the Standard Model
- They can be extremely light
- Constrained if the coupling is large enough by astrophysics, BBN, CMB...

# What If DM Is a Boson and Very Light?

## Dark Matter Particles in the Galaxy



Usually we think of ...

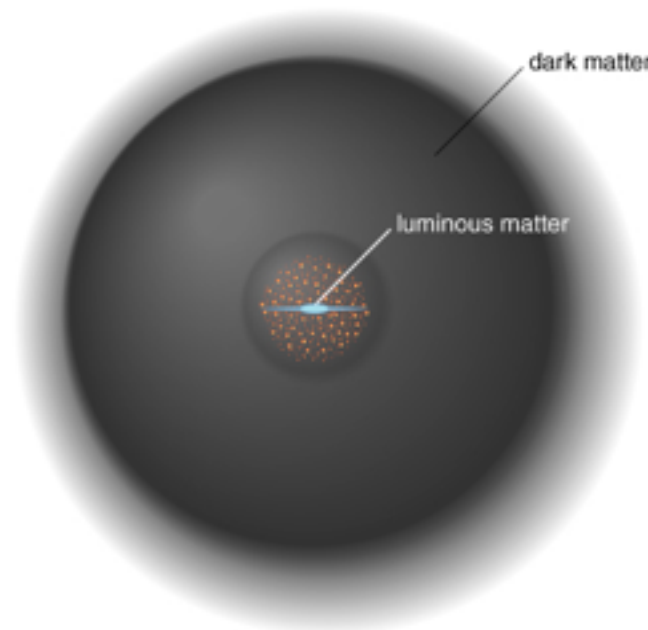


like a WIMP

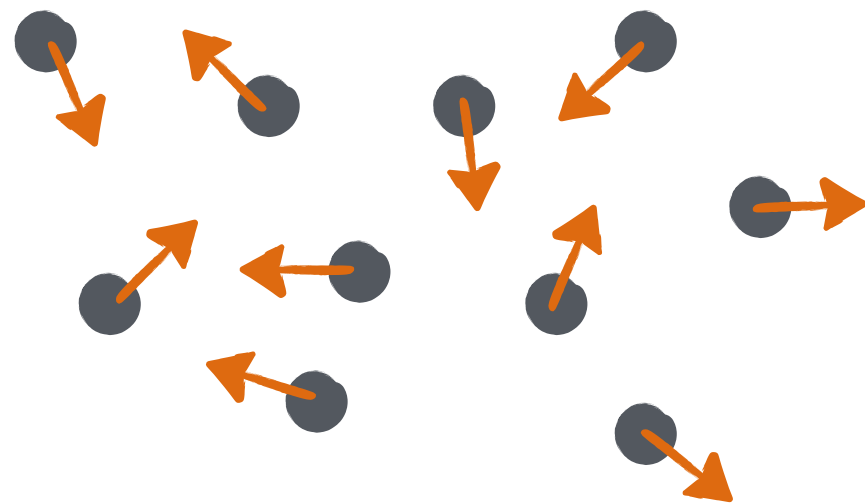


# What If DM Is a Boson and Very Light?

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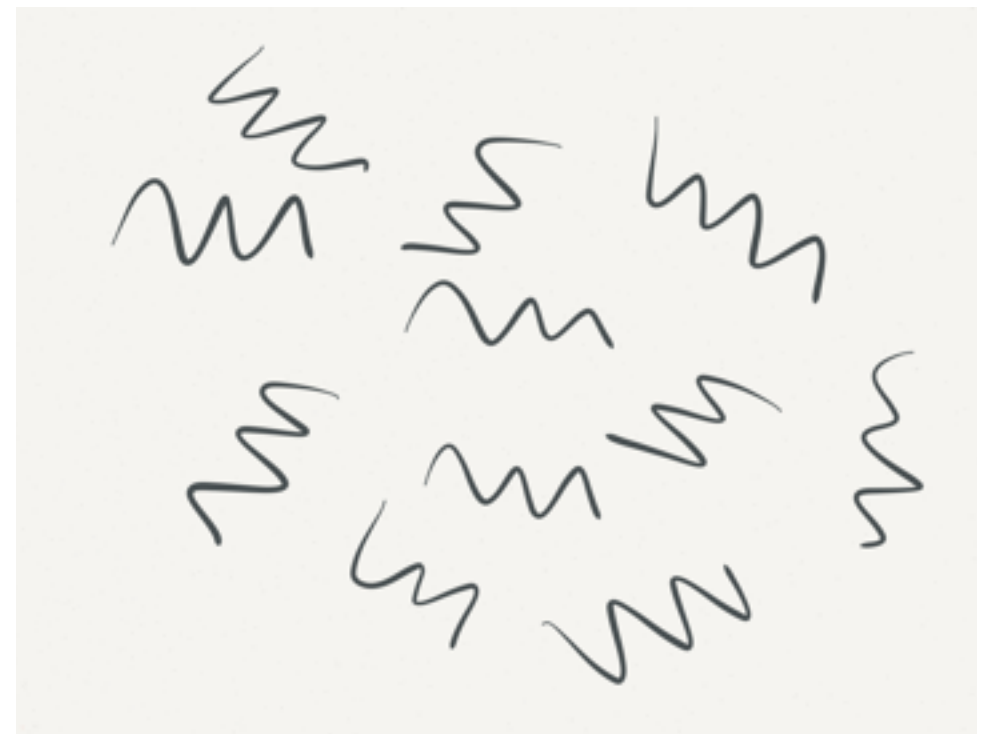


Usually we think of ...



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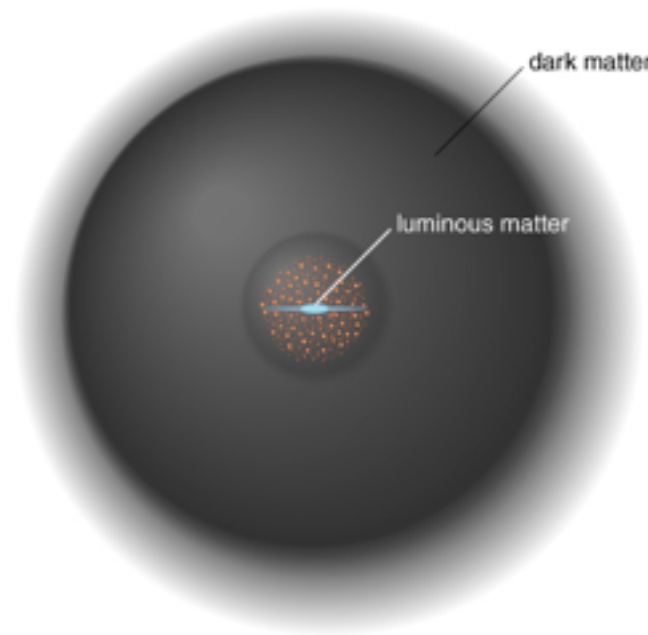
instead of...



$$\lambda_{DM} = \frac{\hbar}{m_{DM}v}$$

# What If DM Is a Boson and Very Light?

## Dark Matter Particles in the Galaxy



Decreasing DM Mass

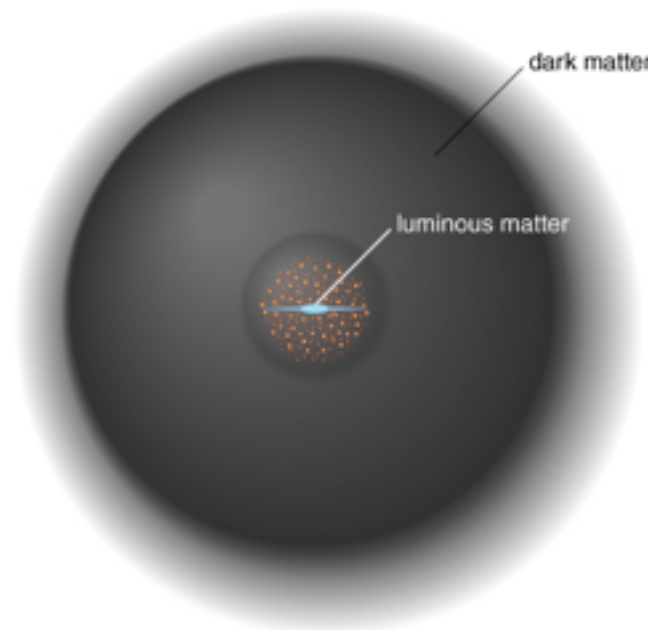


$$\lambda_{DM} = \frac{\hbar}{m_{DM}v}$$



# What If DM Is a Boson and Very Light?

## Dark Matter Particles in the Galaxy



Decreasing DM Mass



$$\lambda_{DM} = \frac{\hbar}{m_{DM}v}$$



Equivalent to a Scalar wave

# Going from DM particles to a DM “wave”



$$\text{When } n_{DM} > \frac{1}{\lambda_{DM}^3}$$

In our galaxy this happens when  $m_{DM} < 1 \text{ eV}/c^2$

we can talk about DM  $\phi(x,t)$  and locally

$$\phi(t) \approx \phi_0 \cos \omega_{DM} t$$

with amplitude

$$\phi_0 \propto \frac{\sqrt{\text{DM density}}}{\text{DM mass}}$$

with frequency

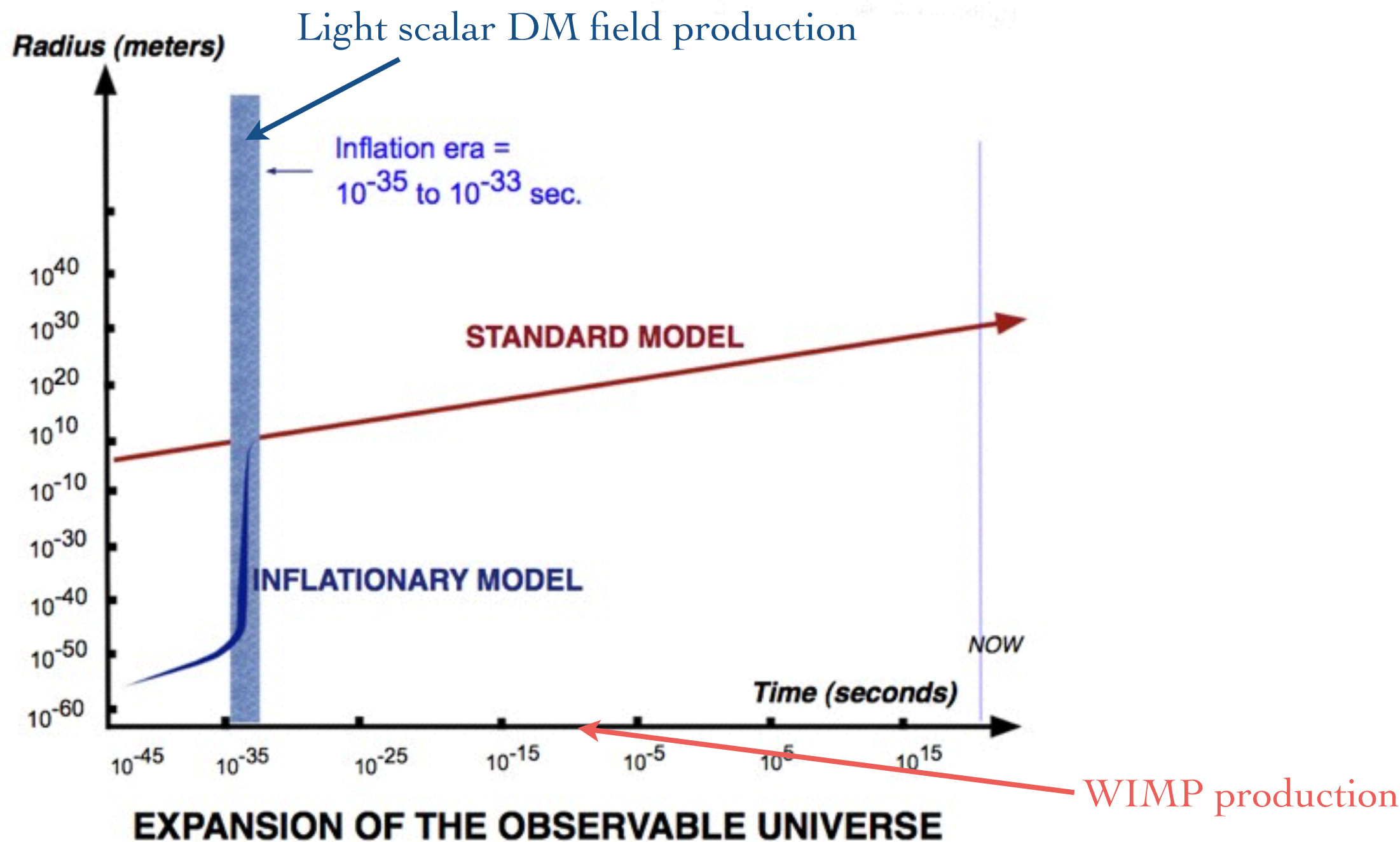
$$\omega_{DM} \approx \frac{m_{DM} c^2}{\hbar}$$

and finite coherence

$$\delta\omega_{DM} \approx \frac{m_{DM} v^2}{\hbar} = 10^{-6} \omega_{DM}$$

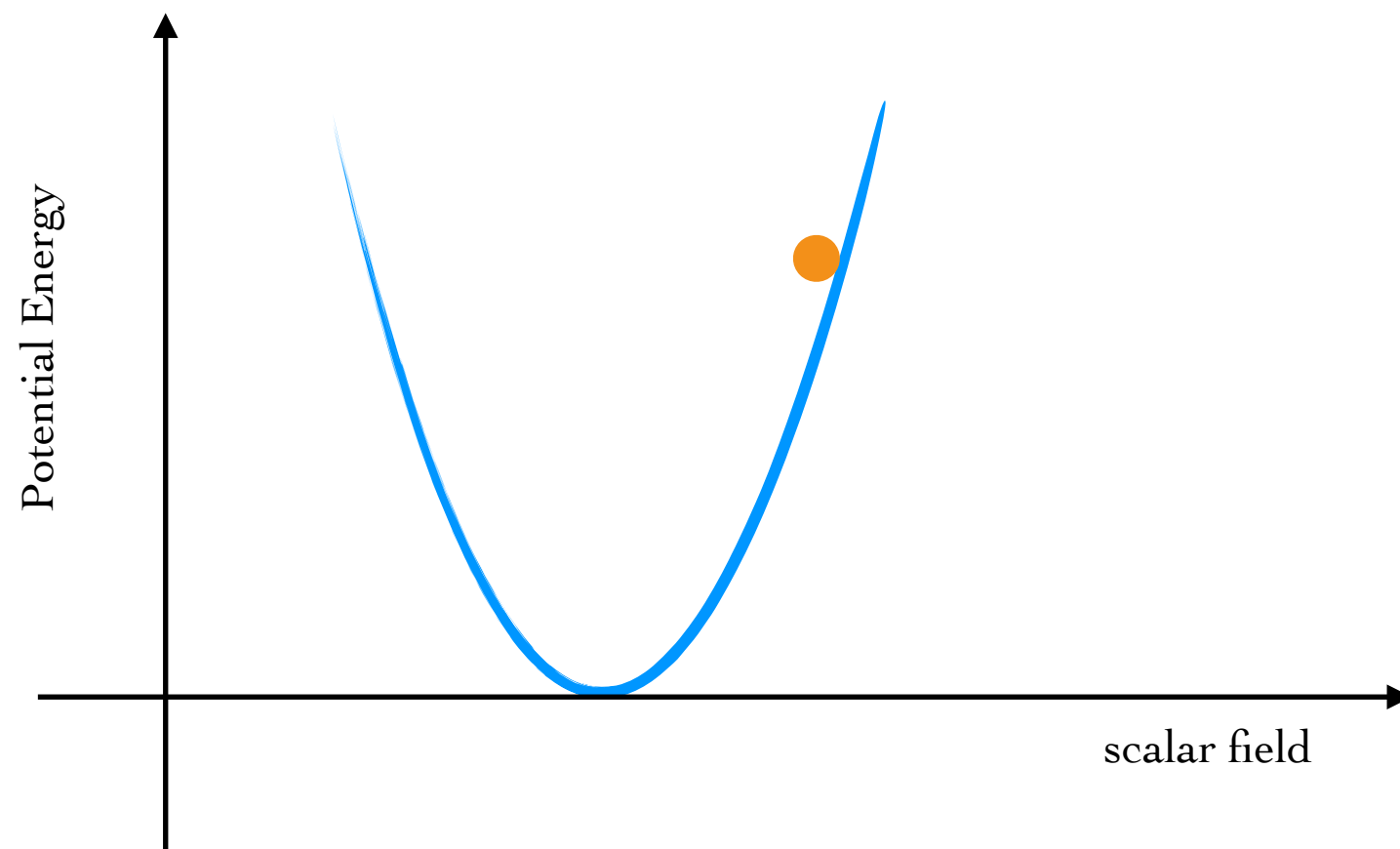
# Scalar DM field Production Mechanism

- The “misalignment mechanism” during inflation



# Light Scalar Dark Matter

- Produced by the misalignment mechanism



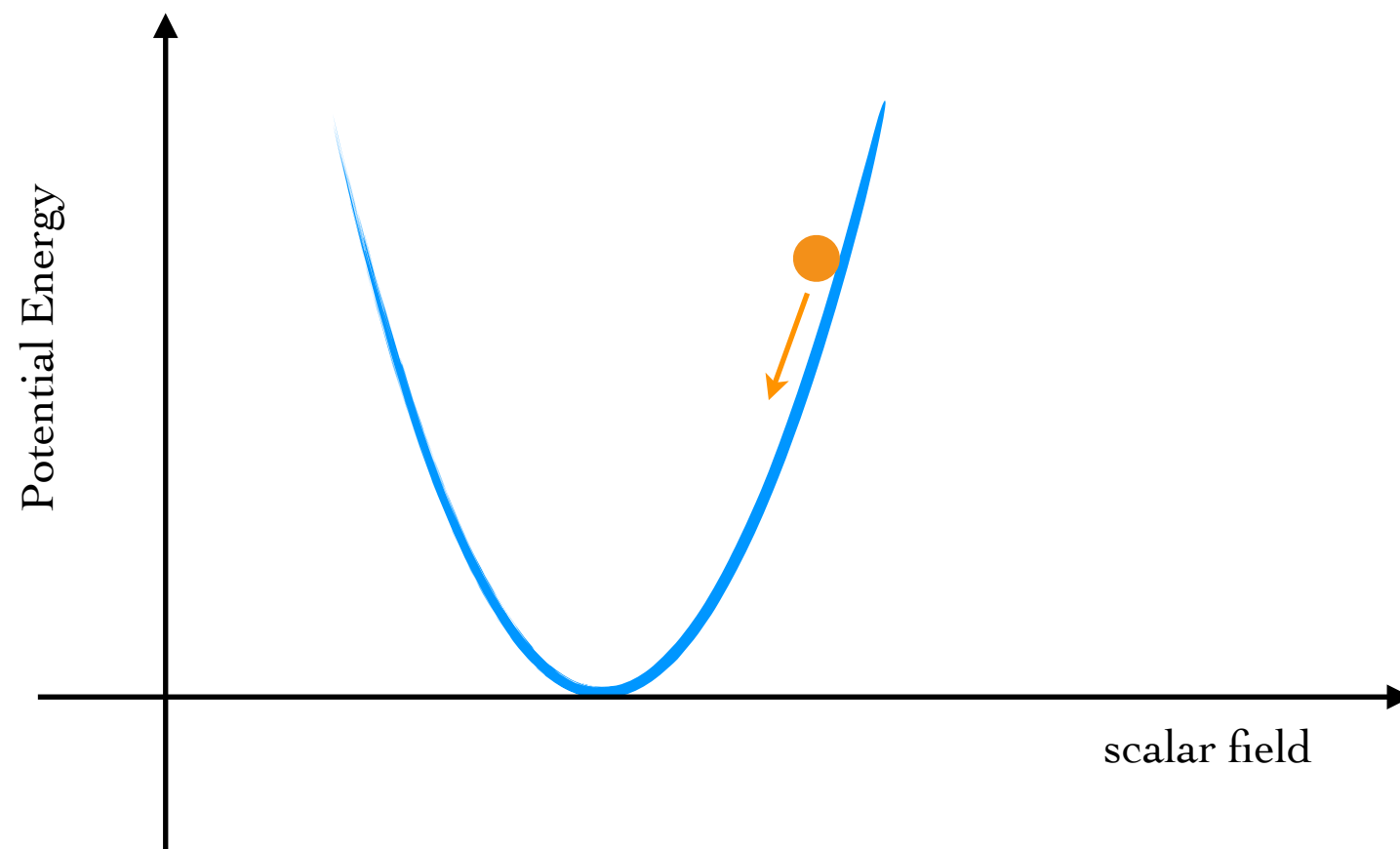
Frozen when:  
 $H_{\text{Hubble}} > m_{\phi}$

Initial conditions set by inflation

\*The story changes slightly if DM is a dark photon

# Light Scalar Dark Matter

- Produced by the misalignment mechanism



Frozen when:  
 $H_{\text{Hubble}} > m_\phi$

Oscillates when:  
 $H_{\text{Hubble}} < m_\phi$

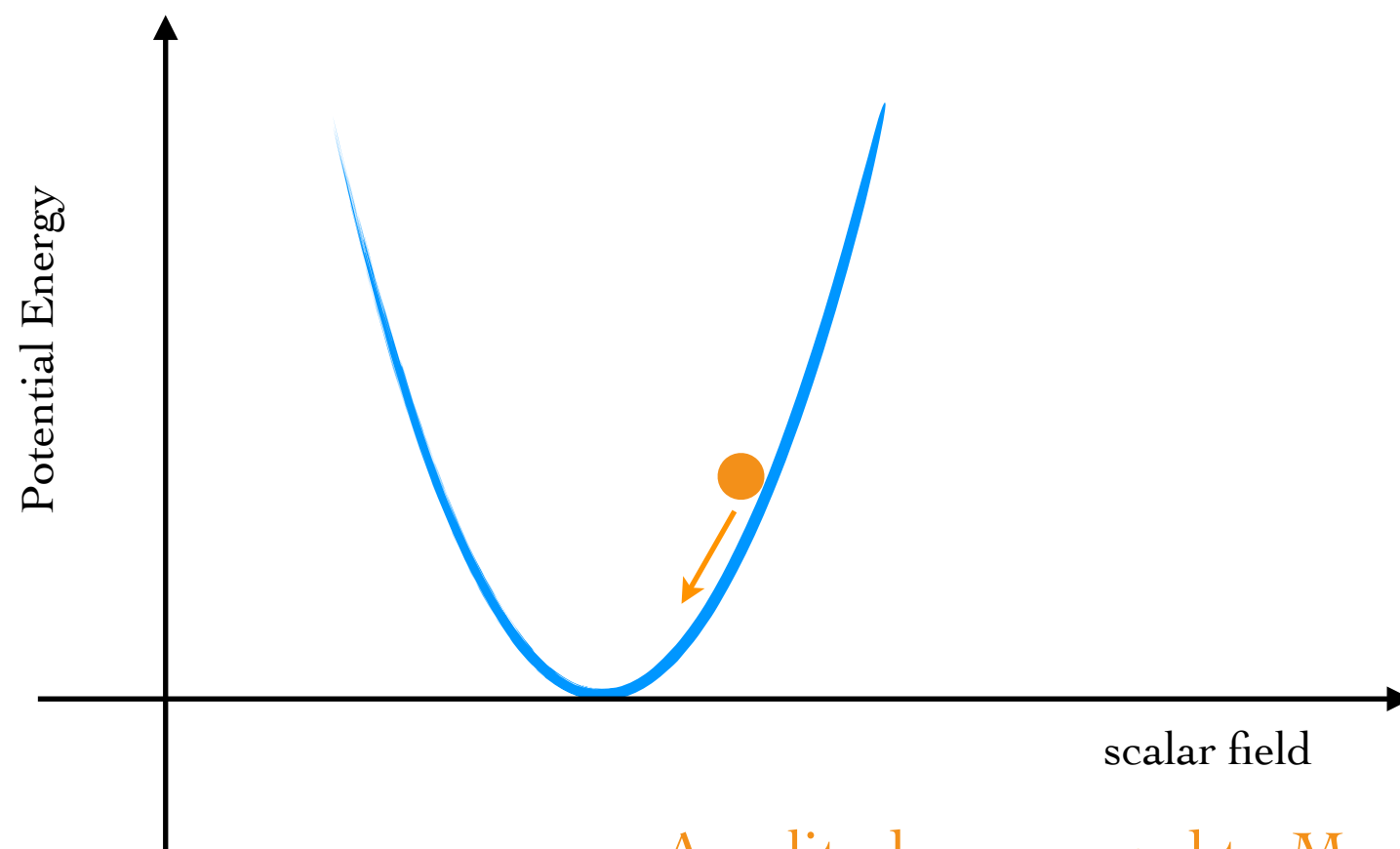
$\rho_\phi$  scales as  $a^{-3}$   
just like **Dark Matter**

Initial conditions set by inflation

\*The story changes slightly if DM is a dark photon

# Light Scalar Dark Matter Today

- If  $m_\phi < 1$  eV, can still be thought of as a scalar field today



$$m_\phi^2 \phi_0^2 \cos^2(m_\phi t) \sim \rho_\phi$$

Coherent for  $v_{\text{vir}}^{-2} \sim 10^6$  periods

Amplitude compared to  $M_{\text{Pl}}$  in the galaxy:

$$\kappa\phi_0 = \frac{\sqrt{8\pi\rho_\phi}}{m_\phi M_{\text{Pl}}} = 6.4 \cdot 10^{-13} \left( \frac{10^{-18} \text{ eV}}{m_\phi} \right)$$



# Axion Dark Matter

- Axion wind (ex. CASPER, QUAX)

$$\mathcal{L} \supset \frac{\vec{\nabla}\phi}{f_\phi} \cdot \vec{\sigma} \quad \text{just like detecting a} \quad \vec{B}_{eff} \equiv \frac{\vec{\nabla}\phi}{\mu_f f_\phi}$$

- Axion-to-photon conversion (ex. ADMX)

$$B_\phi \sim g_{\phi\gamma\gamma} \phi B_{ext}$$

# Dark Photon Dark Matter

- Abundance from inflation depends on  $H_I$

P. W. Graham et al (2015)

$$\Omega_A = \Omega_{\text{cdm}} \times \sqrt{\frac{m}{6 \times 10^{-6} \text{ eV}}} \left( \frac{H_I}{10^{14} \text{ GeV}} \right)^2$$

- Detected if kinetically mixed with the photon

$$\mathcal{L} \supset \epsilon F_{EM} F_{DM}$$

- Detected like a photon (ex. DM Radio)

$$\text{DM electric field} = \text{DM magnetic field} \sim \sqrt{\rho_{DM}}$$

# Moduli Dark Matter

- Moduli set values of measured fundamental constants
- Couple non-derivatively to the Standard Model (as well axions with CP violation)
- Examples of couplings

$$\mathcal{L} = \mathcal{L}_{SM} + \sqrt{\hbar c} \frac{\phi}{\Lambda} \mathcal{O}_{SM}$$

$$\mathcal{O}_{SM} \equiv m_e e \bar{e}, \quad m_q q \bar{q}, \quad G_s^2, \quad F_{EM}^2, \dots$$

Fundamental constants are not really constants

# Oscillating Fundamental Constants

AA, J. Juang, K. Van Tilburg (2014)

From the local oscillation of Dark Matter

Ex. for the electron mass:

$$d_{m_e} \sqrt{\hbar c} \frac{\phi}{M_{Pl}} m_e c^2 e \bar{e}$$

$M_{pl} = 10^{18} \text{ GeV}$   
reduced Planck scale in energy

$$\frac{\delta m_e}{m_e} \approx \frac{d_{m_e} \phi_0}{M_{Pl}} \cos(\omega_{DM} t)$$

$$= 6.4 \times 10^{-13} \cos(\omega_{DM} t) \left( \frac{10^{-18} \text{ eV}}{m_{DM} c^2} \right) \left( \frac{d_{m_e}}{1} \right)$$

$d_{me}$  : coupling strength relative to gravity

Fractional variation set by square root of DM abundance

Need an extremely sensitive probe...

# Ultra-light Scalar Dark Matter

- Mediates new interactions in matter

- Generates a fifth force in matter



- Generates Equivalence Principle violation



# Light Scalar Dark Matter Detection

- Atomic Clocks searches
- Resonant-Mass Detector searches
- Axion Force Experiments
- Detecting ultra-light particles with Astrophysical Black Holes

# Oscillating Atomic and Nuclear Energy Splittings due to Dark Matter

- Optical Splittings

$$\Delta E_{\text{optical}} \propto \alpha_{EM}^2 m_e \sim \text{eV}$$

- Hyperfine Splittings

$$\Delta E_{\text{hyperfine}} \propto \Delta E_{\text{optical}} \alpha_{EM}^2 \left( \frac{m_e}{m_p} \right) \sim 10^{-6} \text{ eV}$$

- Nuclear Splittings

$$\Delta E (m_p, \alpha_s, \alpha_{EM}) \sim 1 \text{ MeV}$$

DM appears as a signature in atomic (or nuclear) clocks

# Atomic Clocks

- Kept tuned to an atomic energy level splitting

**Current definition of a second:**

the duration of 9192631770 periods of the radiation  
corresponding to the transition between the two hyperfine levels  
of the ground state of the caesium 133 atom

- Have shown stability of 1 part in  $10^{18}$

Compared to 1 part in  $10^{13}$  expected by DM

- Have won several Nobel prizes in the past 20 years

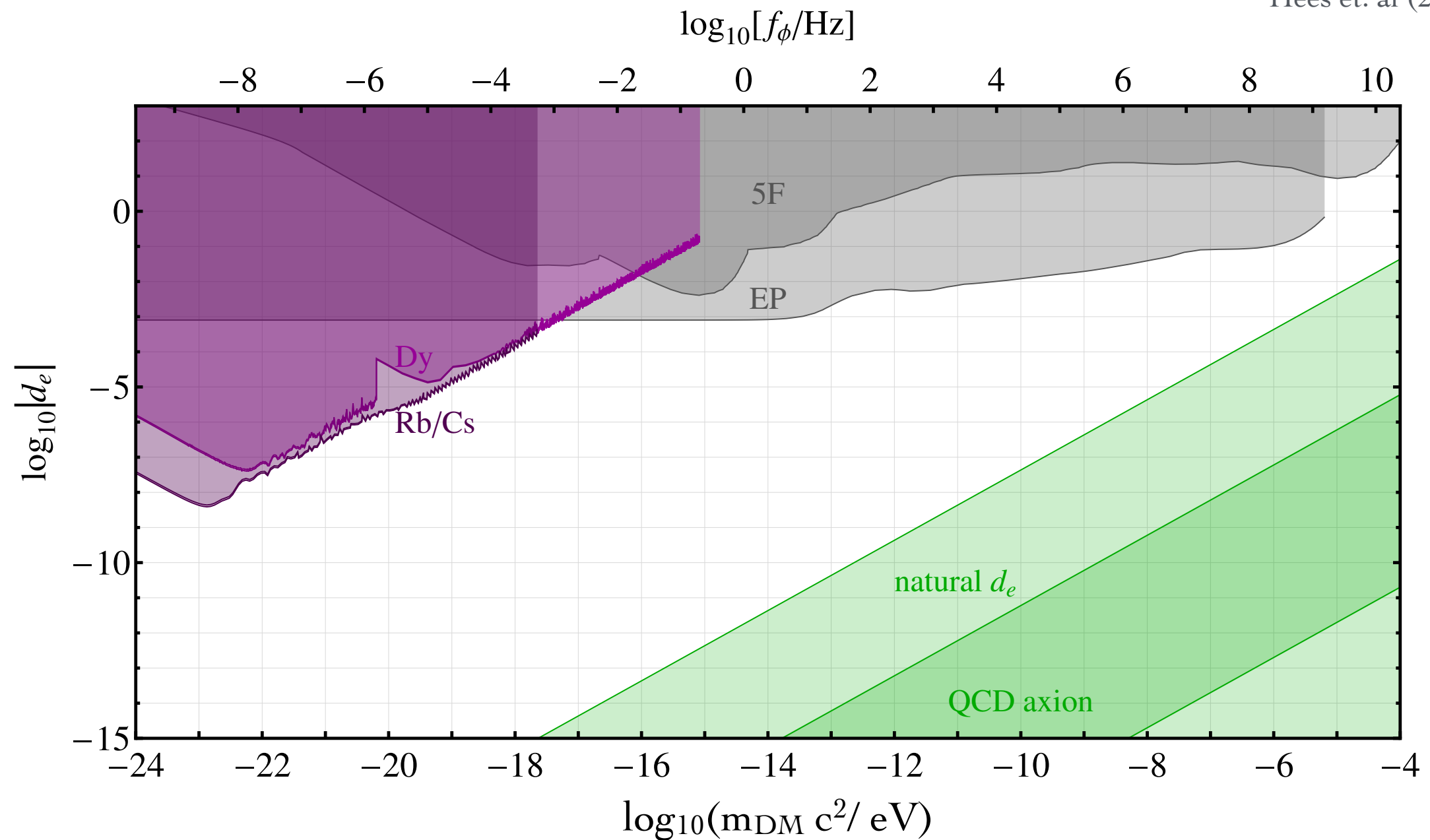


# The Dy isotope and Rb/Cs Clock Comparison

Ken Van Tilburg  
and the Budker group (2015)

sensitivity to  $\alpha_{\text{EM}}$  variations

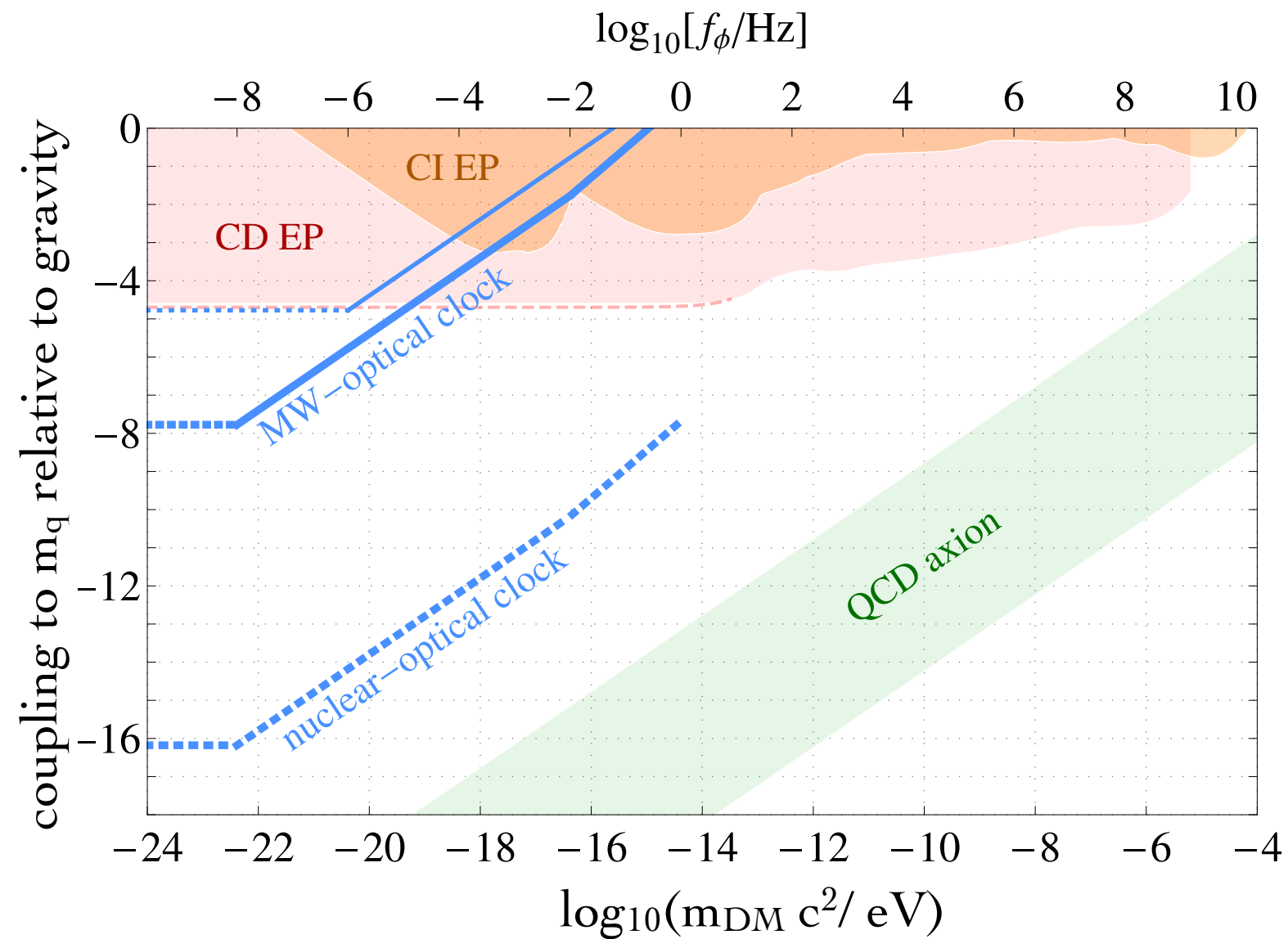
Hees et. al (2016)



Analysis performed with existing data

# Nuclear to Optical Clock Comparison

Future Sensitivity of a  $^{229}\text{Th}$  clock



# Oscillating interatomic distances

- The Bohr radius changes with DM

- $r_B \sim (\alpha m_e)^{-1}$

$$\frac{\delta r_B}{r_B} = - \left( \frac{\delta \alpha_{EM}}{\alpha_{EM}} + \frac{\delta m_e}{m_e} \right)$$

- The size of solids changes with DM

- $L \sim N (\alpha m_e)^{-1}$

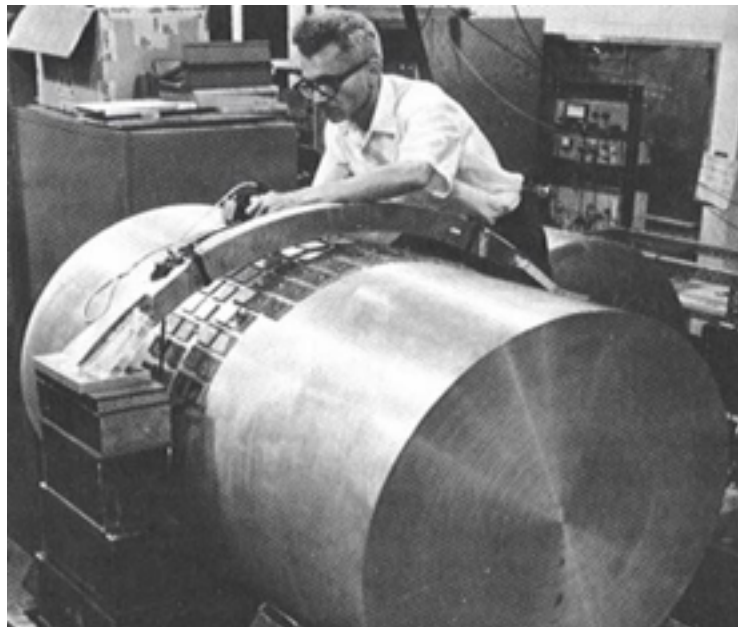
$$\frac{\delta L}{L} = - \left( \frac{\delta \alpha_{EM}}{\alpha_{EM}} + \frac{\delta m_e}{m_e} \right)$$

For a single atom  $\delta r_B \sim 10^{-30}$  m

Need macroscopic objects to get a detectable signal

# Resonant-Mass Detectors

- In the 1960's: **The Weber Bar**



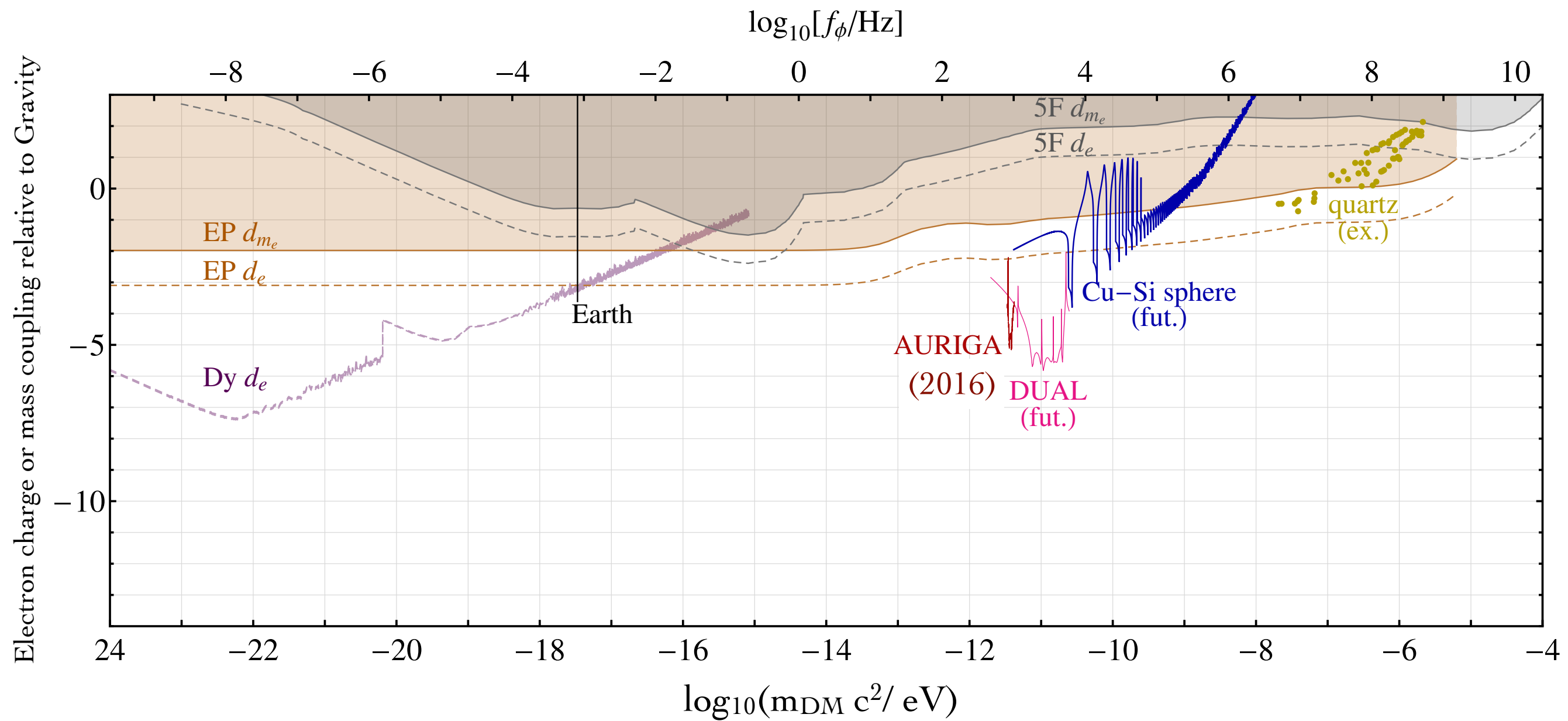
Fractional length variation  $\delta L/L \sim 10^{-17}$

- Today: AURIGA, NAUTILUS, MiniGrail

Fractional length variation  $\delta L/L \sim 10^{-23}$



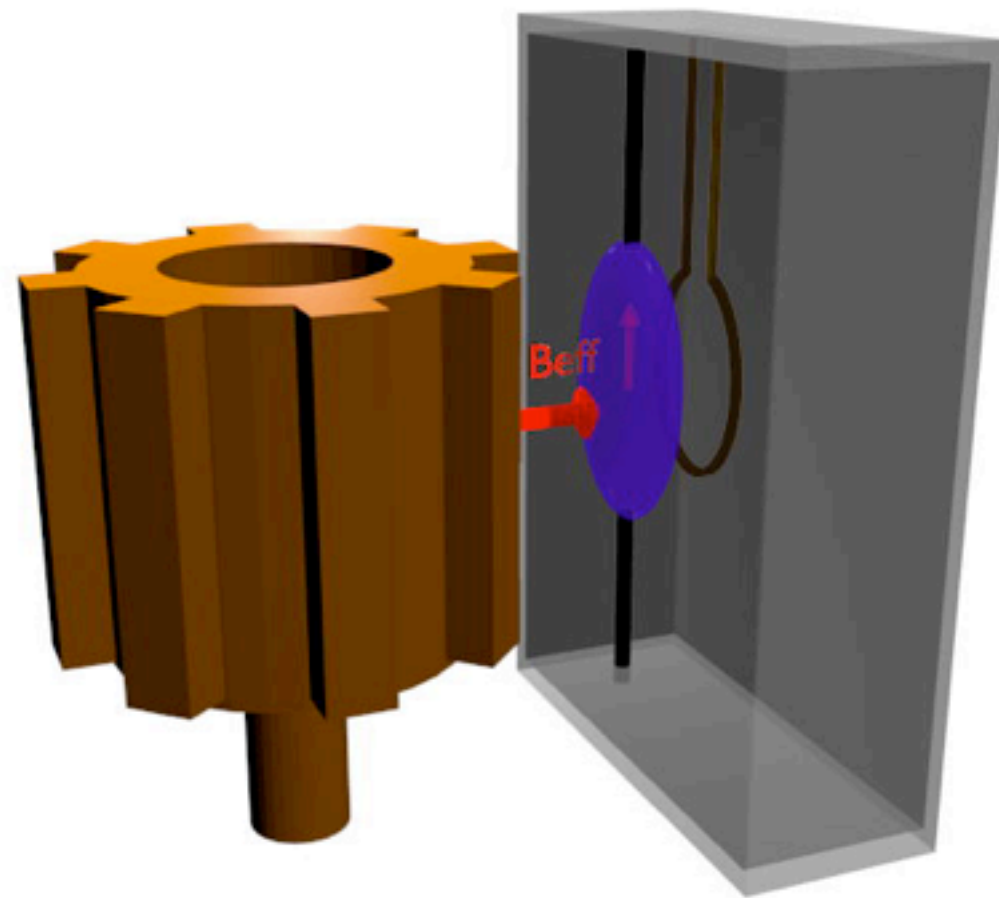
# What can be done in the future?



ARIADNE:  
Axion Resonant InterAction Detection Experiment  
with Andrew Geraci (2014)  
and A. Kapitulnik, Chen-Yu Liu, J. Long, Y. Semertzidis, M. Snow (to be built)

# ARIADNE:

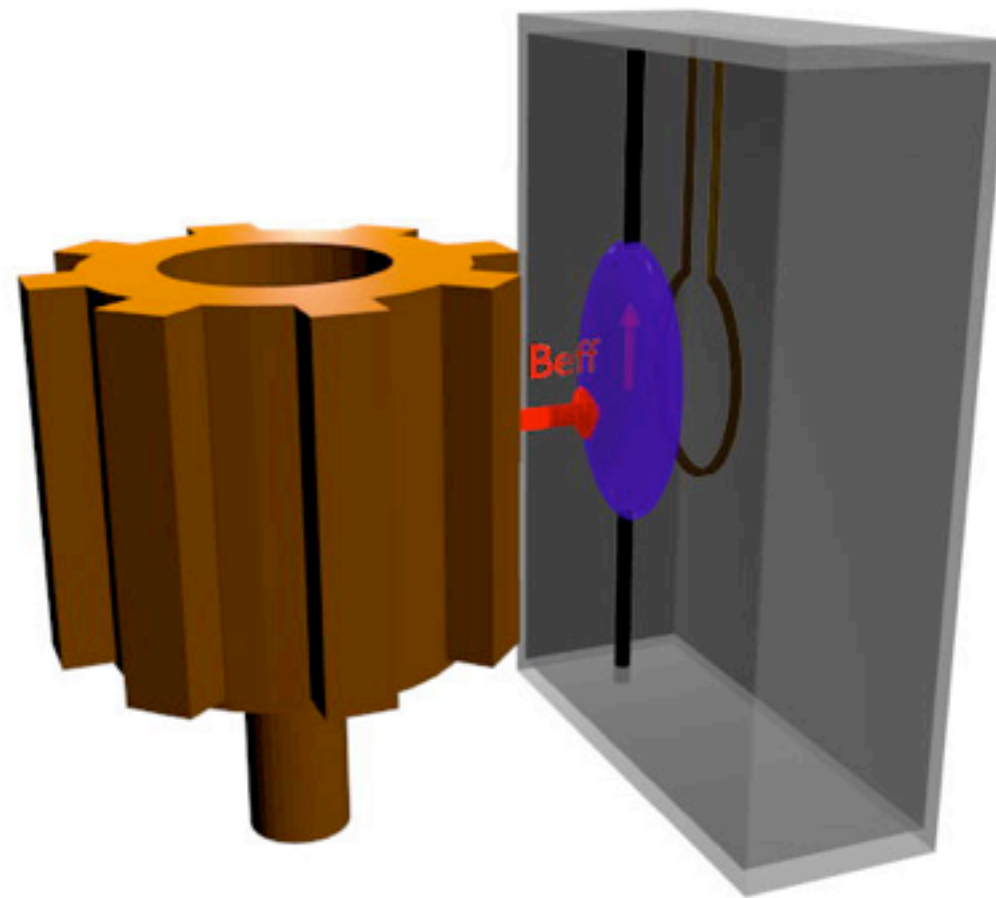
## Axion Resonant InterAction DetectionN Experiment



He-3 NMR sample with  
 $T_2$  up to  $\sim 1000$  sec

# ARIADNE:

## Axion Resonant InterAction DetectionN Experiment



He-3 NMR sample with  
 $T_2$  up to ~1000 sec

$$B_{\min} \approx p^{-1} \sqrt{\frac{2\hbar b}{n_s \mu_{3\text{He}} \gamma V T_2}} = 3 \times 10^{-19} \text{ T} \times$$

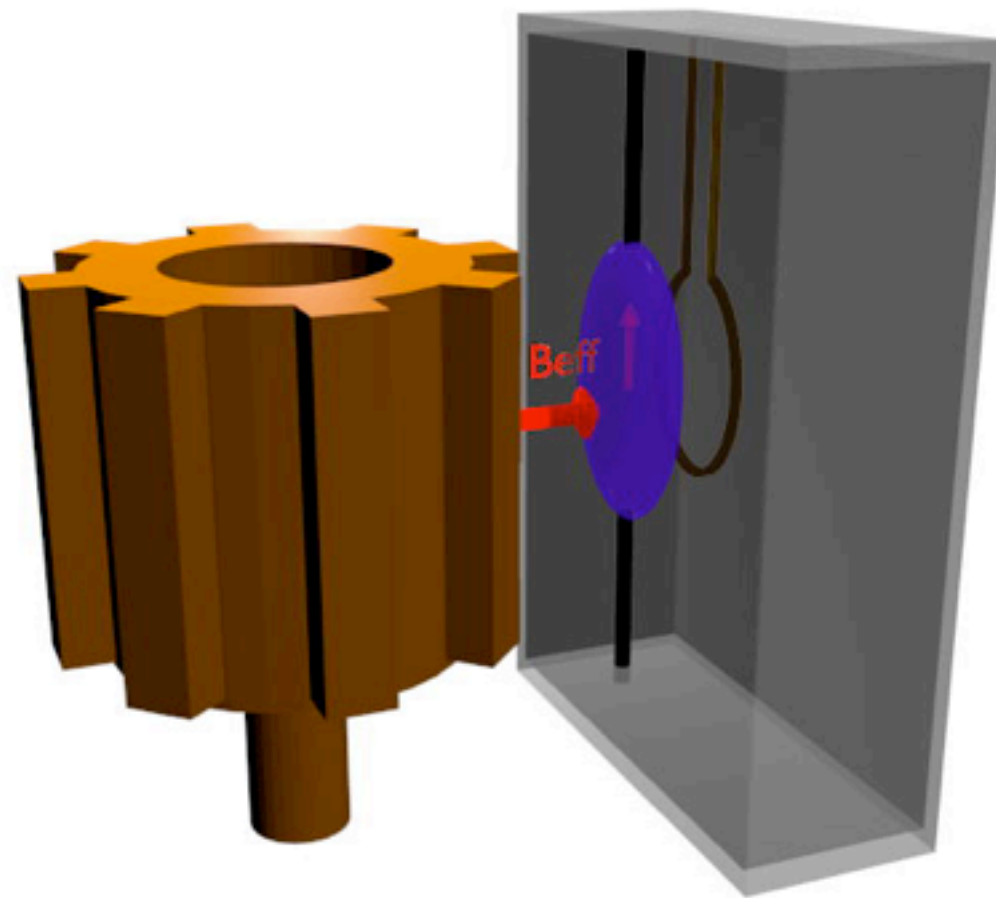
$$\left(\frac{1}{p}\right) \sqrt{\left(\frac{b}{1 \text{ Hz}}\right) \left(\frac{1 \text{ mm}^3}{V}\right) \left(\frac{10^{21} \text{ cm}^{-3}}{n_s}\right) \left(\frac{1000 \text{ s}}{T_2}\right)}$$

$B_{\min} = 10^{-16} \text{ T}/(\text{Hz})^{1/2}$   
 for SQUIDs



# ARIADNE:

## Axion Resonant InterAction DetectionN Experiment



He-3 NMR sample with  
 $T_2$  up to ~1000 sec

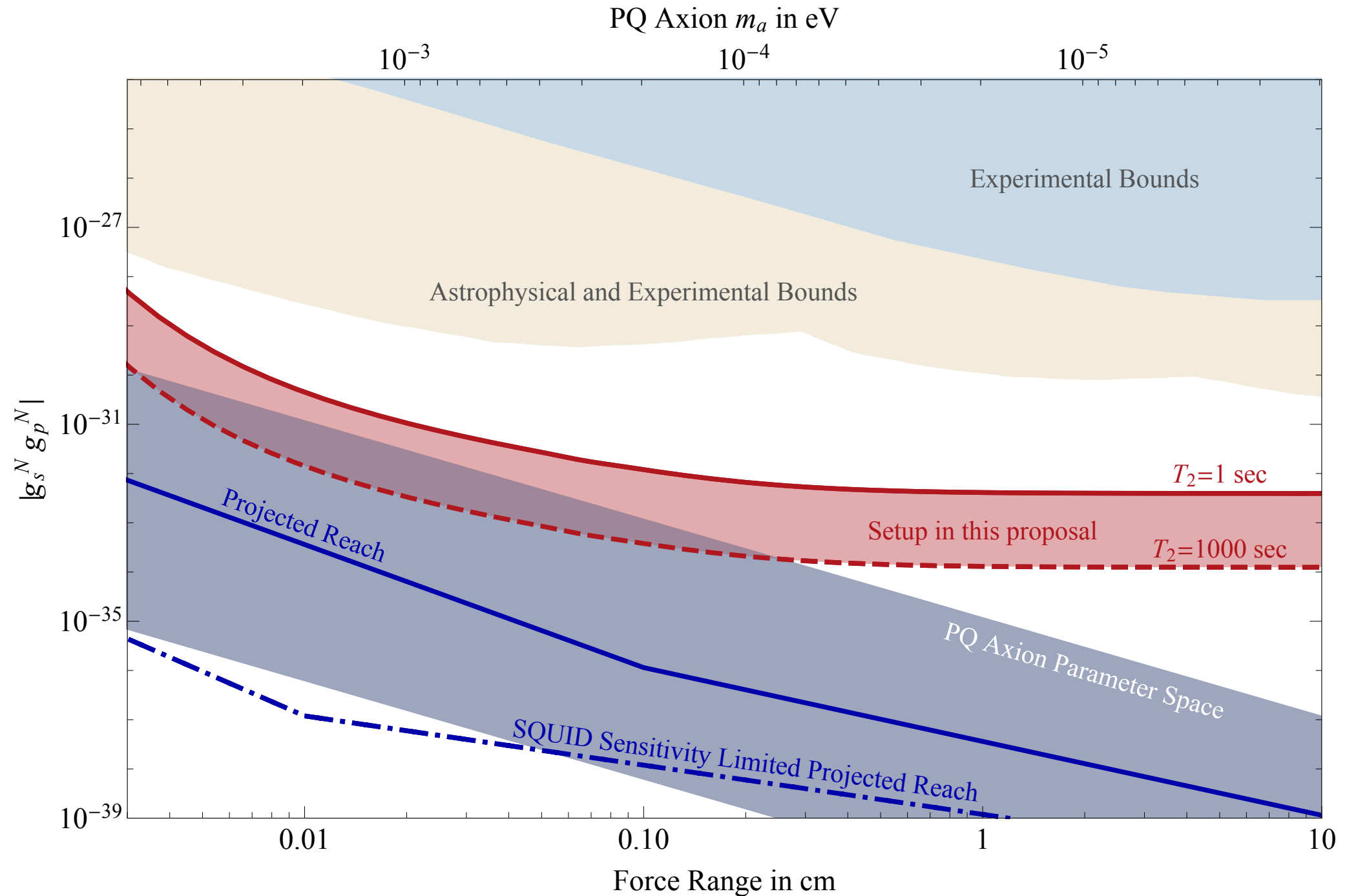
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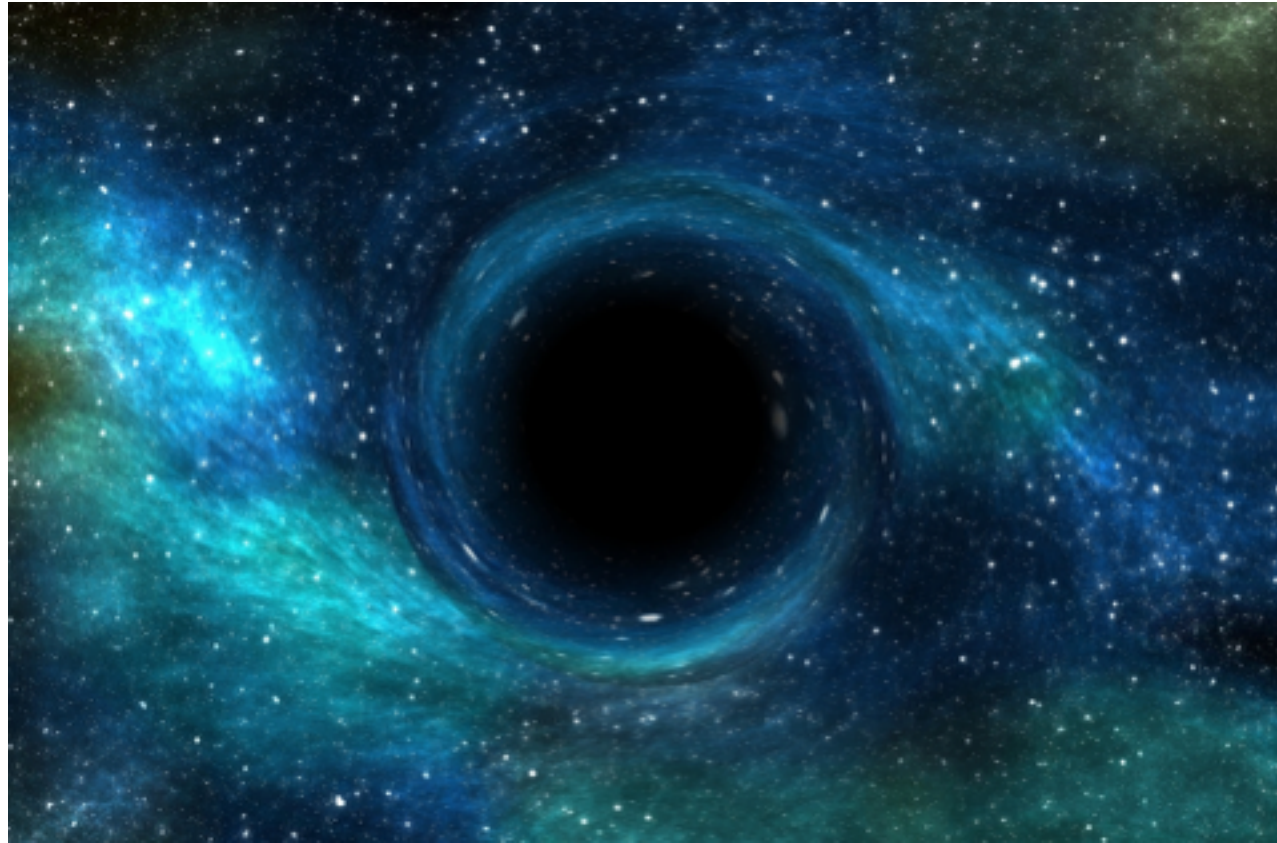
# Monopole-Dipole Interaction Reach

Unpolarized Source Mass with  $10^6$  sec integration



Projected Reach with increase of polarized spin density  
and larger NMR sample volume

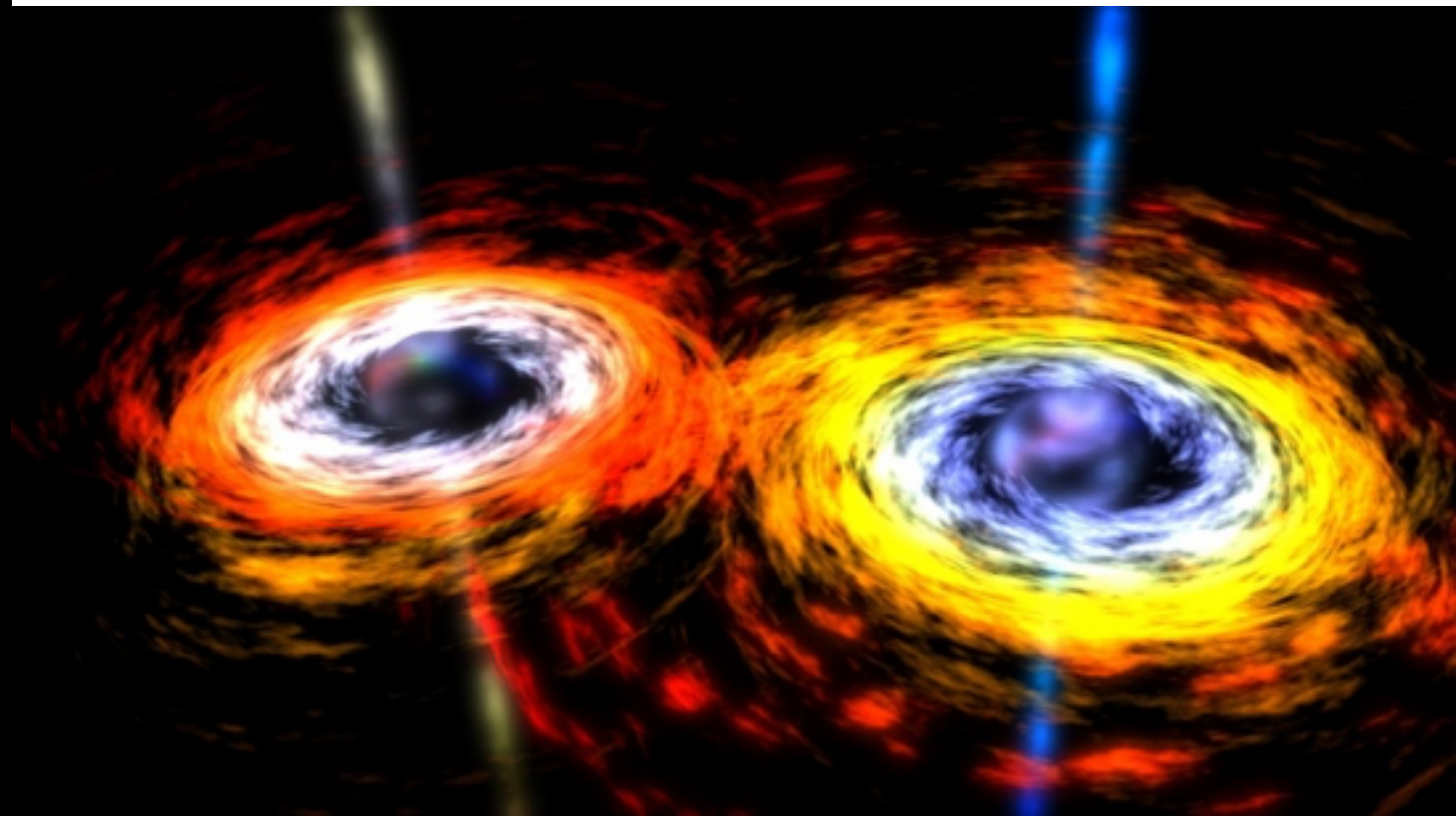
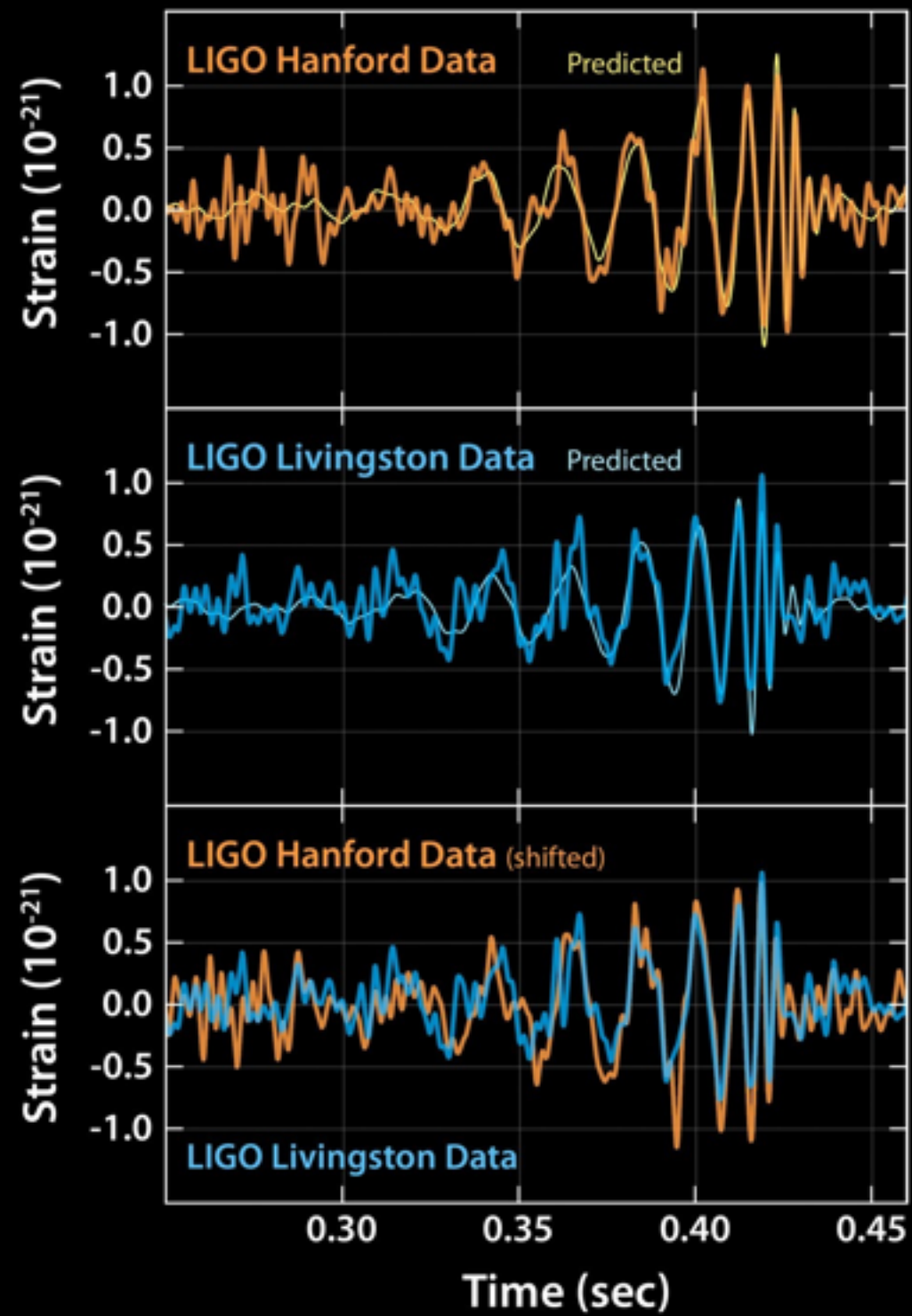
# Black Holes as Nature's Detectors



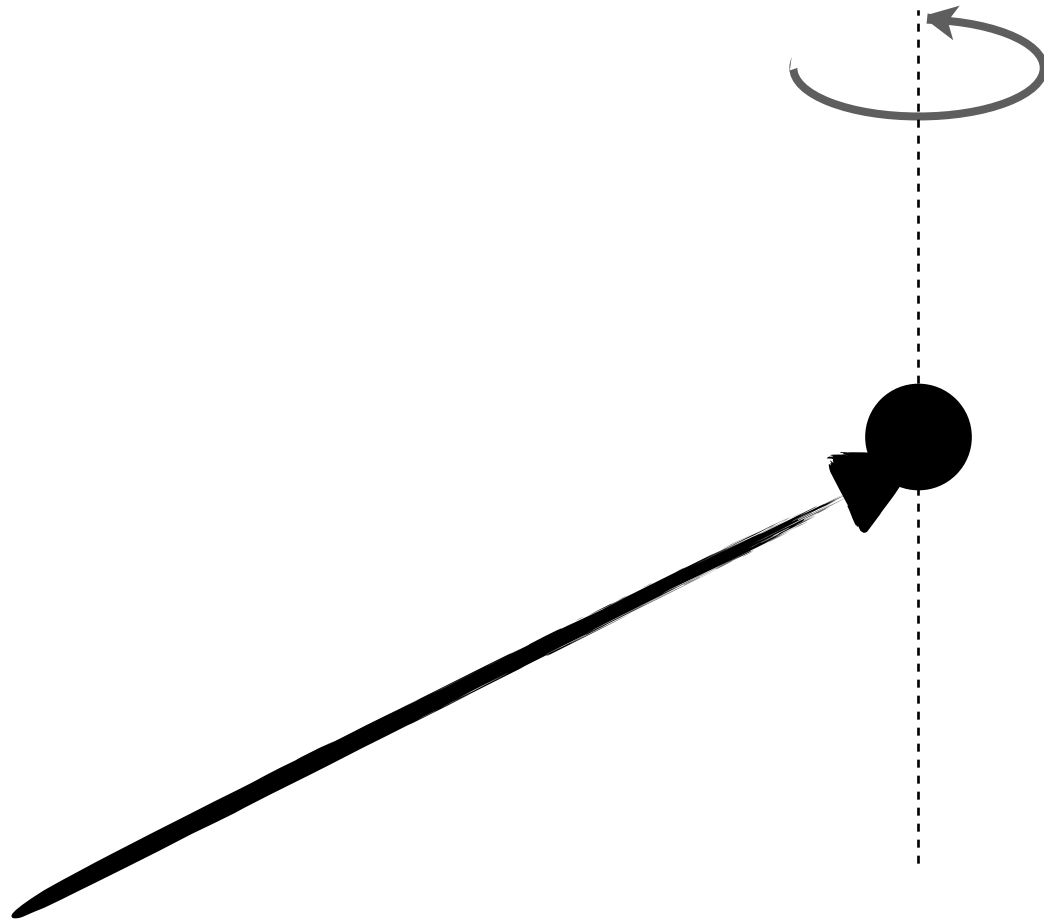
1 km -10 billion km

They can detect bosons of similar in size

September 14, 2015



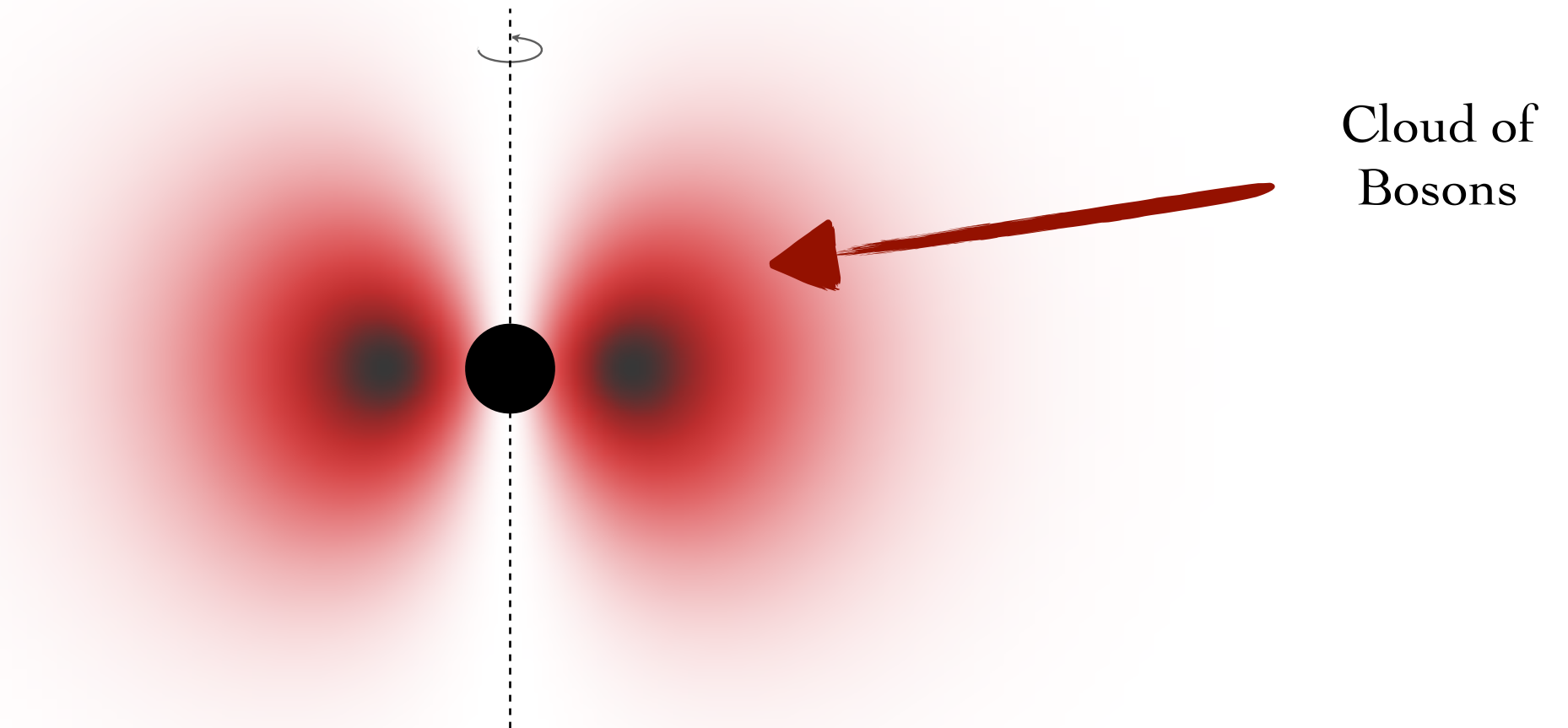
# Superradiance and The Gravitational Atom in the Sky



Rotating Black Hole



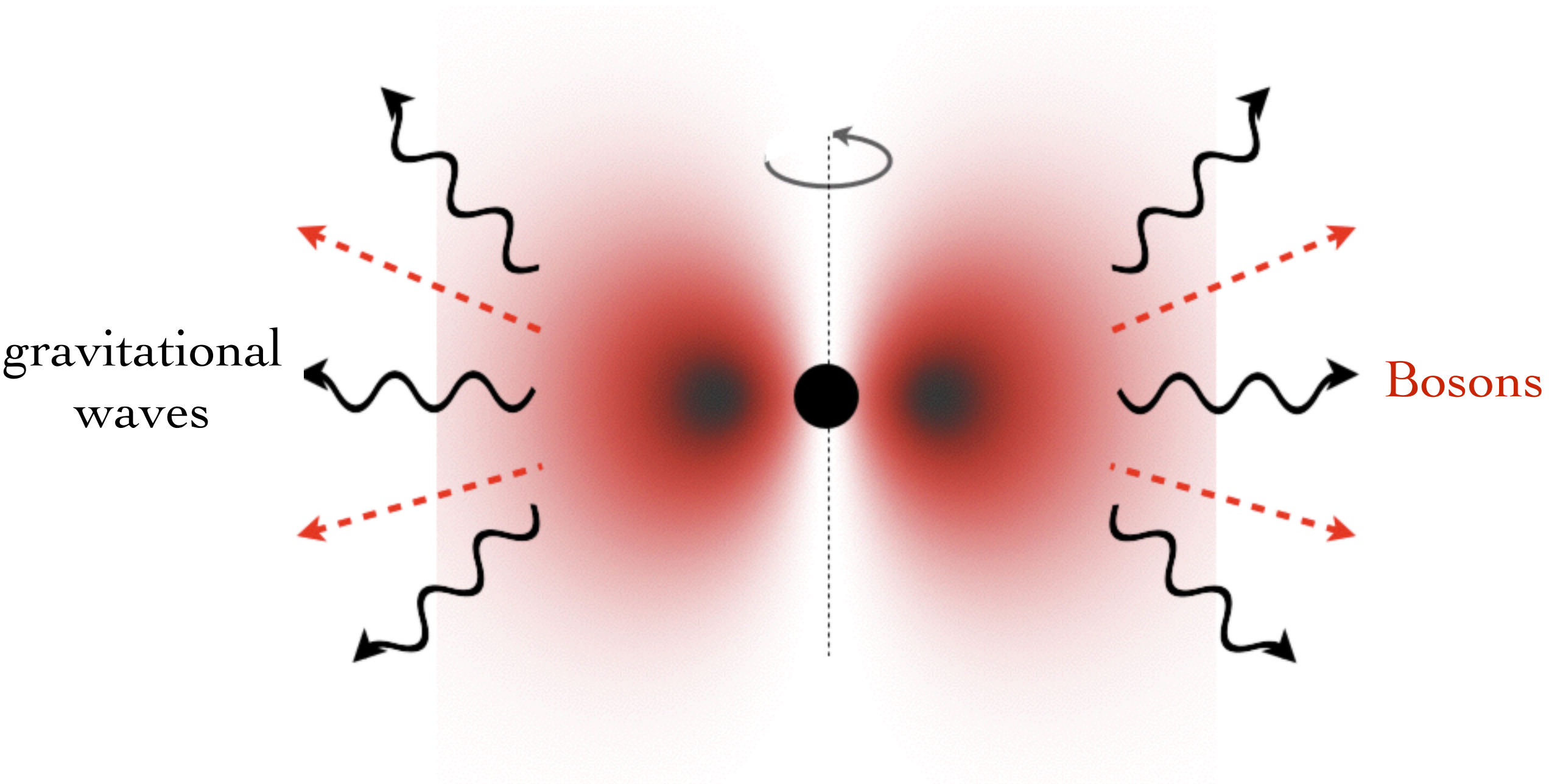
# Superradiance and The Gravitational Atom in the Sky



Particles Occupying the Same Bound Orbit:

Can be comparable to the number of protons in all the stars in the universe

# A Gravitational Wave Laser in The Sky



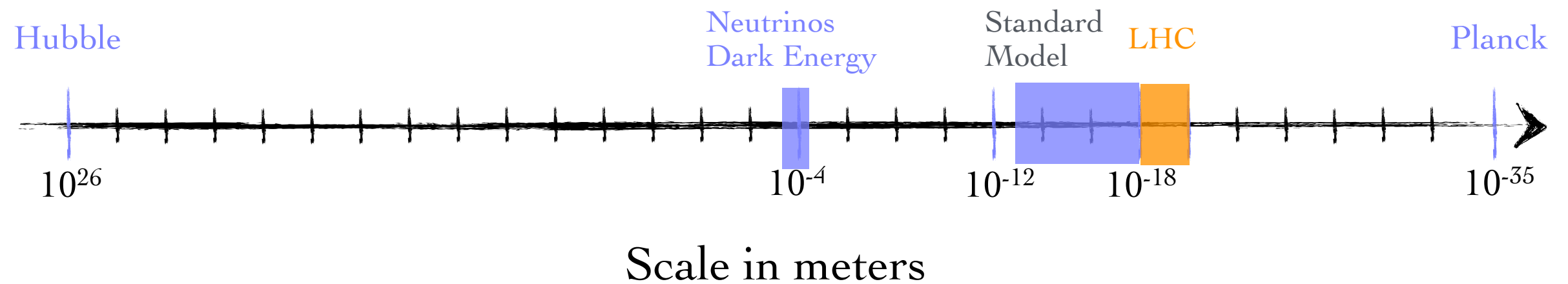
# Summary

- There is excellent theoretical motivation for boson DM candidates below 1 eV in mass
- Correlated with observations across many experiments

This is only scratching the surface...



# The Precision Frontier



There are more things in heaven and earth, Horatio,  
Than are dreamt of in your philosophy.  
- Hamlet